

Chiral amplitudes for two jets processes in quasi-peripheral kinematics

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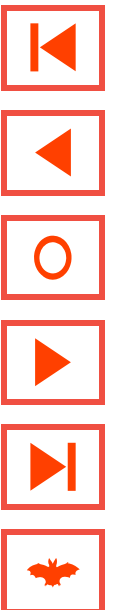
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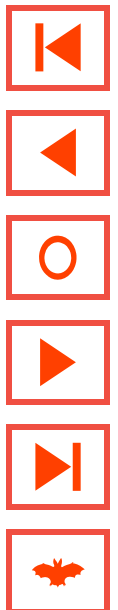
Outlook

- Introduction - ILC
- Quasiperipheral kinematics
- Impact factors
- Radiative corrections
- Conclusions

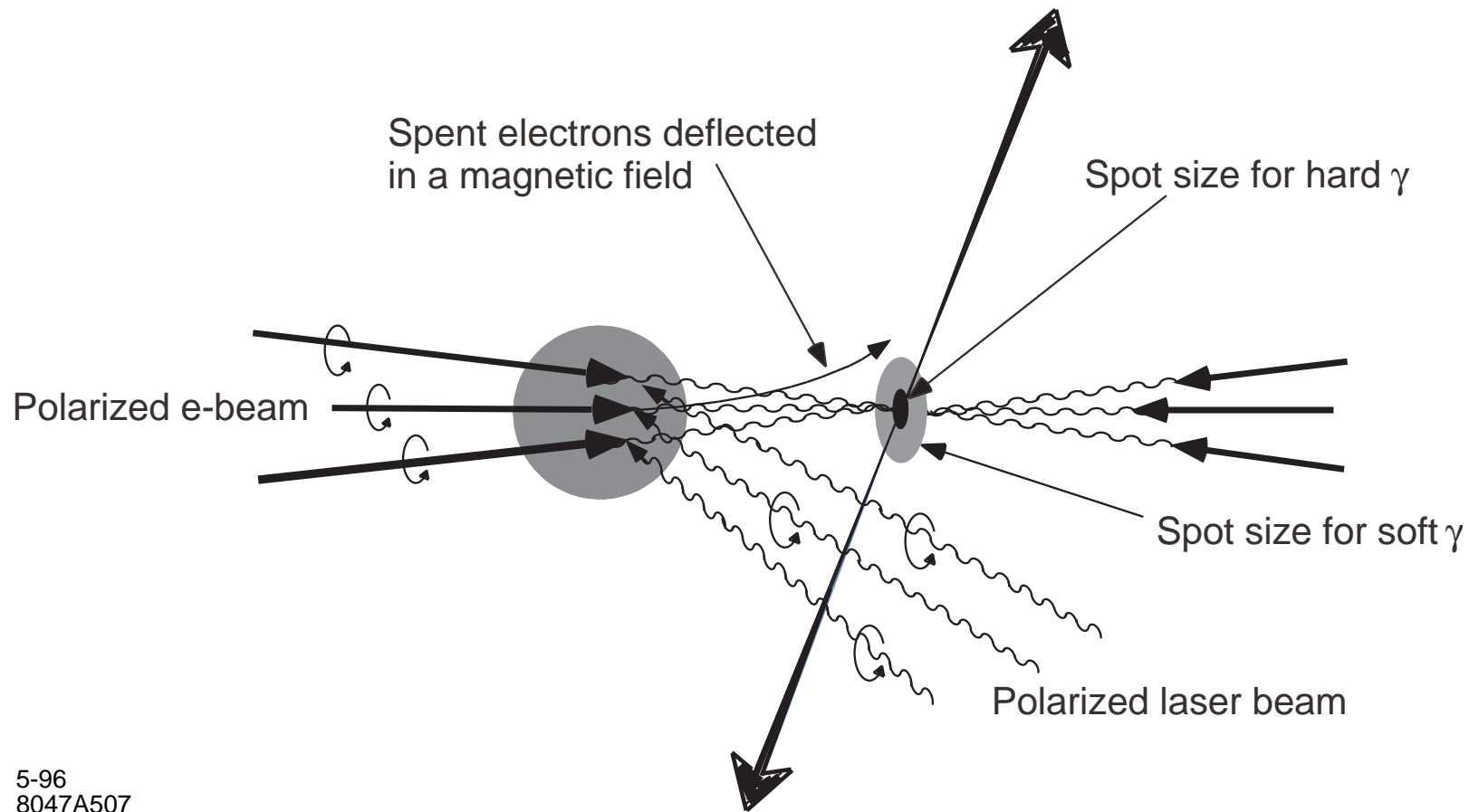


Relevant Works

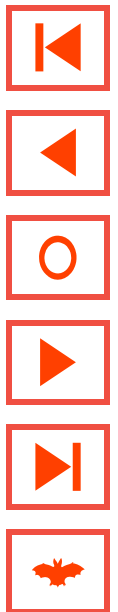
- V. Bytev, E. Bartos, M. V. Galynskii and E. A. Kuraev,
“Radiative corrections to chiral amplitudes in quasiperipheral kinematics,”
J. Exp. Theor. Phys. **103**, 224 (2006).
- E. Bartos, M. V. Galynsky, S. R. Gevorkian and E. A. Kuraev,
“QED calibration processes for polarized gamma–gamma and gamma–e- colliders,”
Phys. Part. Nucl. **35**, S90 (2004).
- E. Bartos, A. Z. Dubnickova, M. V. Galynskii and E. A. Kuraev,
“Calibration processes for photon–photon colliders,”
Nucl. Phys. B **676**, 481 (2004).



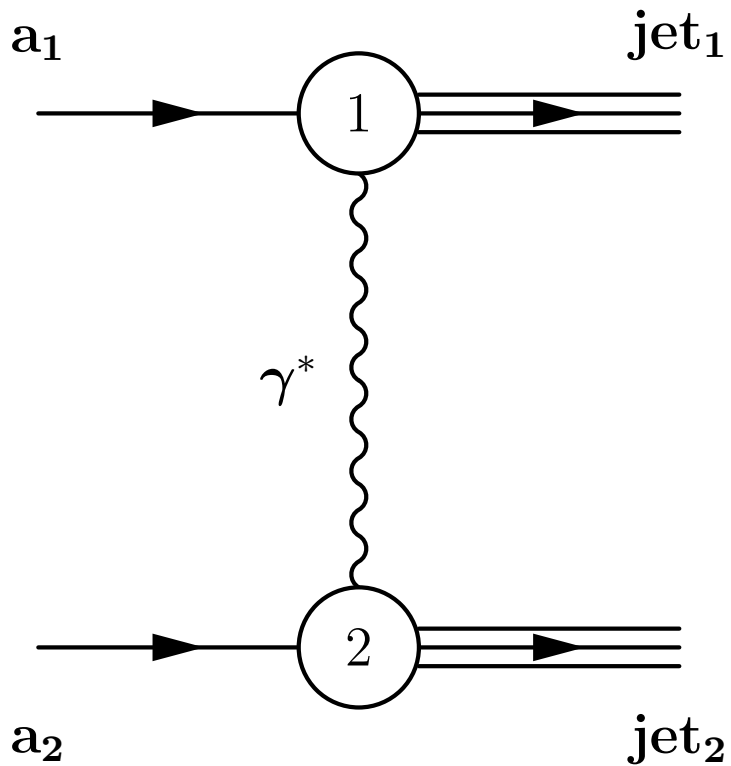
International Linear Collider



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Considered QED processes

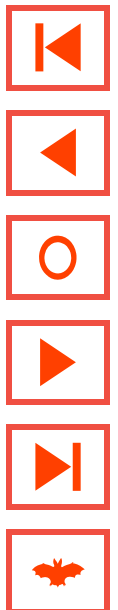


$$a_1(p_1, \delta_1) + a_2(p_2, \delta_2) \rightarrow \text{jet}_1^{(\lambda_1)} + \text{jet}_2^{(\lambda_2)}$$

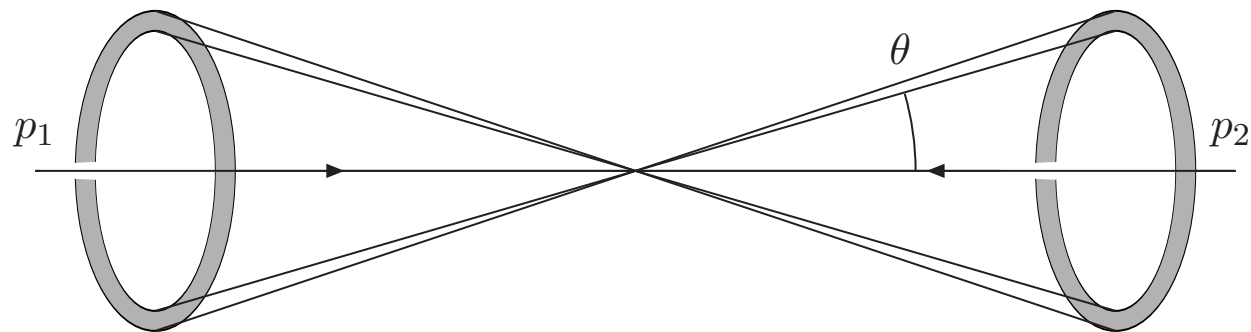
$$a_{1,2} = e^\pm, \gamma,$$

$$(p_1 + p_2)^2 = s \gg m_i^2,$$

- Processes could be studied at high energy collisions of initial particles in **peripheral kinematics**, i.e. small angles θ of emission of jet particles to the direction of its parent particle
- **Significant property** of processes: their differential and total crossing sections do not decrease with c.m.s. total energy \sqrt{s}
- Corresponding cross sections of the relevant QED processes are **large numerically** \Rightarrow essential background in studying of weak and strong interactions. Moreover, could serve for monitoring and calibration purposes.
- Unfortunately, small θ -s are very **hard measurable**.



Quasiperipheral (QP) kinematics



- $\frac{2m_i}{\sqrt{s}} \ll \theta_i \ll 1$ – provides the independence on energy of differential cross sections but have an accuracy of order of θ^2 , so comparable with the accuracy of peripheral kinematics contribution.
- independence of spin states of a_1 -jet₁ and a_2 -jet₂ blocks of process (we can put $\delta_{1,2} = +1$) → consequence of Gribov's decomposition of metric tensor

Generalized form of the amplitude

$$M^{(12)} = i s \frac{\delta \pi \alpha}{\mathbf{q}^2} \Phi_1 \Phi_2,$$

$$\Phi_1 = \frac{1}{s} J^{1,\mu} p_{2\mu}, \quad \Phi_2 = \frac{1}{s} J^{2,\nu} p_{1\nu}.$$

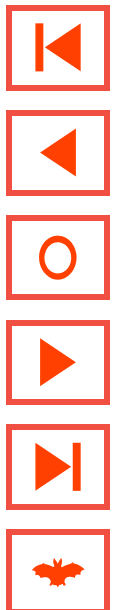
J^i – currents for blocks 1,2

Φ_i – their light-cone projections: $\Phi_{1,2}(\mathbf{q}) \rightarrow 0$ if $|\mathbf{q}| \rightarrow 0$

We used Sudakov's parametrization of 4-momenta

$$p_{i1} = \alpha_i p_2 + x_i p_1 + p_{\perp i1}, \quad p_{j2} = y_j p_2 + \beta_j p_1 + p_{\perp j2},$$

$$q = \alpha p_2 + \beta p_1 + q_{\perp}, \quad q^2 \approx -\mathbf{q}^2$$

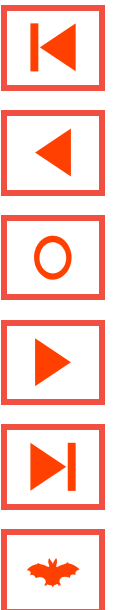


The differential cross section written in terms of impact factors

$$\int d\sigma^{(12)} = \frac{\alpha^2}{\pi^2} \frac{d^2 \mathbf{q}}{(\mathbf{q}^2)^2} \int d\tau_1^{\lambda_1} \int d\tau_2^{\lambda_2},$$

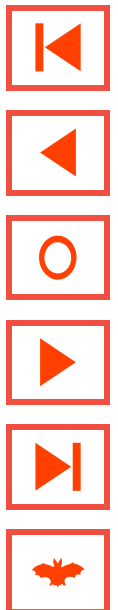
$$\int d\tau_i^{(\lambda_i)} = \int |\Phi_i^{(\lambda_i)}(q)|^2 d\Gamma_i, \quad i = 1, 2.$$

Impact factors $\int d\tau_i$ do not depend on s .



Helicity states

- F. A. Berends, R. Kleiss, P. De Causmaecker, R. Gastmans, W. Troost and T. T. Wu,
“Multiple Bremsstrahlung In Gauge Theories At High-Energies. 2. Single Bremsstrahlung,”
Nucl. Phys. B **206** (1982) 61.
- F. A. Berends, R. Kleiss, P. De Causmaecker, R. Gastmans and T. T. Wu,
“Single Bremsstrahlung Processes In Gauge Theories,”
Phys. Lett. B **103** (1981) 124.



Conversion of the initial photon with momentum p_1 and helicity λ

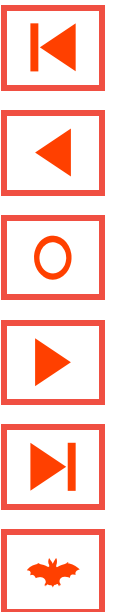
$$\gamma^*(q) + \gamma(p_1, \lambda) \rightarrow e^+(q_+) + e^-(q_-, \sigma)$$

$$\hat{\varepsilon}^\lambda(p_1) = N_\gamma(\hat{q}_- \hat{q}_+ \hat{p}_1 \omega_{-\lambda} - \hat{p}_1 \hat{q}_- \hat{q}_+ \omega_\lambda),$$

$$(\varepsilon^\lambda)^2 = 0, \quad (\varepsilon^\lambda \varepsilon^{-\lambda}) = -1, \quad \omega_\sigma = \frac{1 + \sigma \gamma_5}{2}, \quad \sigma = \pm 1.$$

Helicity states of fermions are defined as $u^\sigma = \omega_{-\sigma} u$, $v^\sigma = \omega_\sigma v$.

$$\Phi_B^{\gamma,++} \sim \bar{u}(q_-) \omega_{-\hat{q}_+ \hat{q}} \frac{\hat{p}_2}{s} \omega_+ v(q_+) \rightarrow \int d\tau_B^{\gamma,++} = \frac{\alpha}{\pi} \int \frac{d^2 q_- dx_-}{x_+ x_-} \frac{\mathbf{q}^2 x_+^2}{\chi_+ \chi_-}$$



Other subprocesses in Born approximation

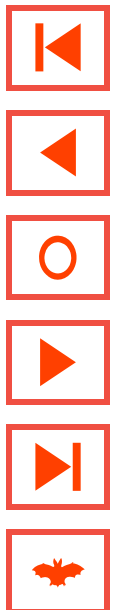
$$\gamma(p_1, \lambda = +) + e^-(p_2, \eta) \rightarrow e^+(q_+, \mp) + e^-(q_-, \pm) + e^-(p'_2, \eta)$$

$$\frac{d\sigma_{\eta}^{\gamma,++}}{d\Gamma} = \frac{d\sigma_{\eta}^{\gamma,--}}{d\Gamma} = \frac{2x_+^2 \alpha^3}{\pi^2 \mathbf{q}^2 \chi_+ \chi_-},$$

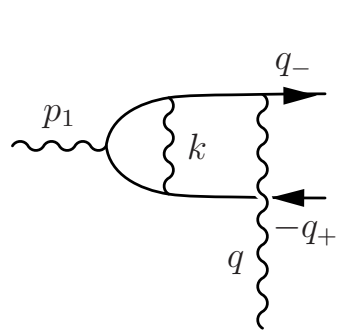
$$\frac{d\sigma_{\eta}^{\gamma,+ -}}{d\Gamma} = \frac{d\sigma_{\eta}^{\gamma,- +}}{d\Gamma} = \frac{2x_-^2 \alpha^3}{\pi^2 \mathbf{q}^2 \chi_+ \chi_-}, \quad d\Gamma = \frac{d^2 q d^2 q_- dx_-}{x_+ x_-}.$$

Similarly for the process

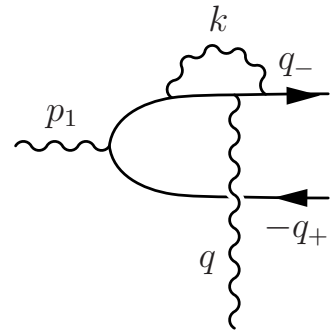
$$e^-(p_2, \eta) + e^-(p_1, \sigma = +) \rightarrow e^-(p'_1, +) + \gamma(k_1, \lambda = \pm) + e^-(p'_2, \eta)$$



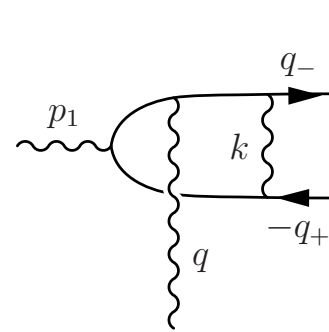
Photon impact factor



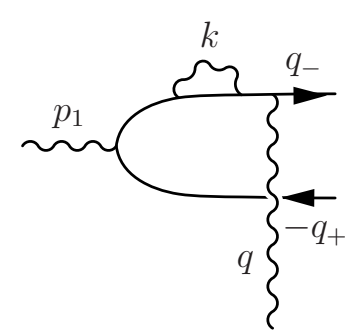
a



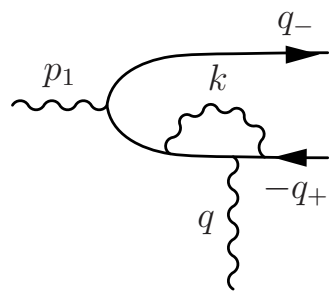
b



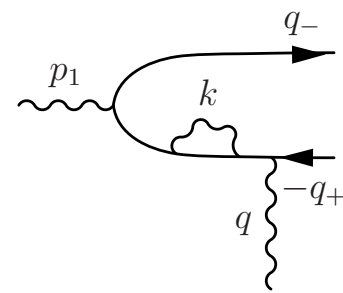
c



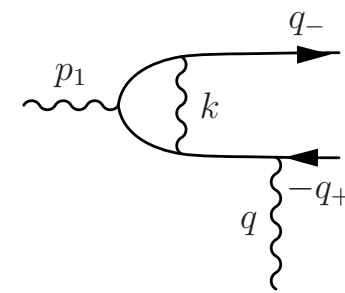
d



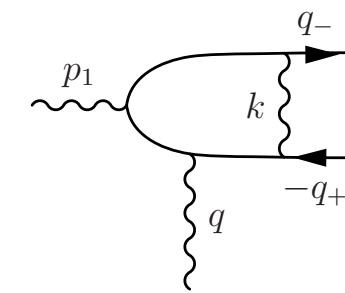
e



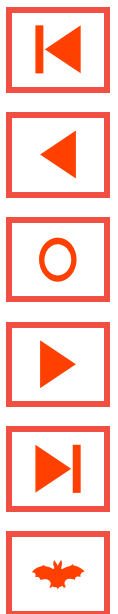
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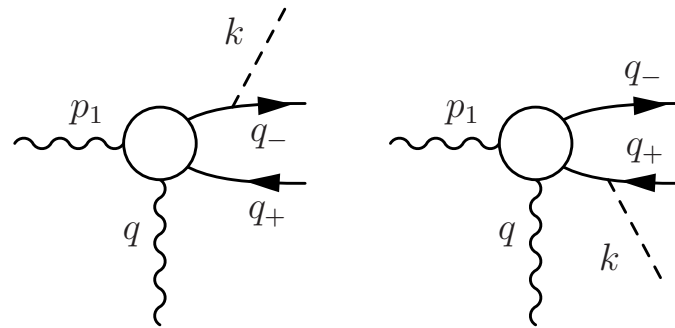


g



h

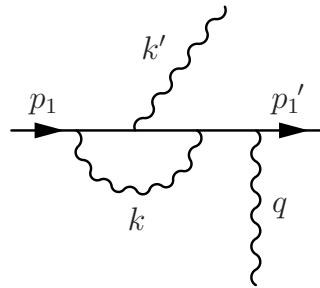




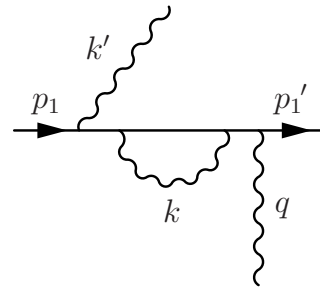
$$\begin{aligned}
 d\sigma^\gamma &= 2[d\tau_{\pm, \text{box}}^{\gamma, +\pm} + d\tau_{\mp, \Sigma V}^{\gamma, +\pm} + d\tau_{\mp, V}^{\gamma, +\pm}] + d\tau_{\text{soft}}^{\gamma, +\pm} \\
 &= \frac{\alpha}{2\pi} d\tau_B^{\gamma, \pm} [(l_s - 1)(\ln \Delta + 3 - 2 \ln(x_+ x_-)) + K_{SV}^{\gamma, \pm}], \\
 \Delta &= \Delta\epsilon / \epsilon_\gamma, \quad l_s = \ln(s_1 / m^2)
 \end{aligned}$$

- K factor - next-to-leading terms
- r.h.s. $\rightarrow 0$ if $q^2 \rightarrow 0$ (check of calculation)

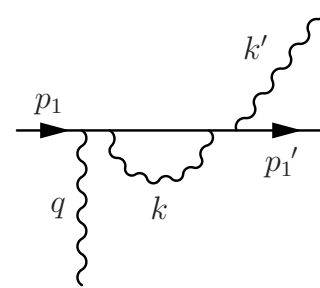
Electron impact factor



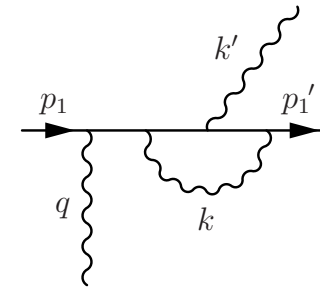
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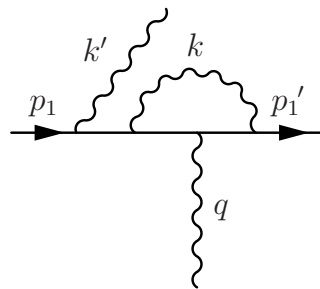
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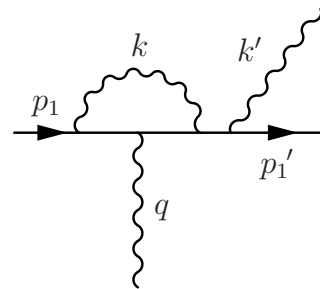
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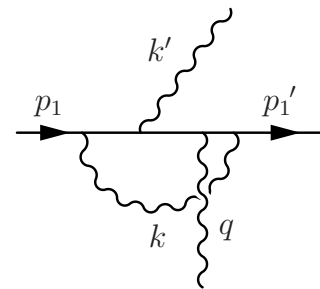
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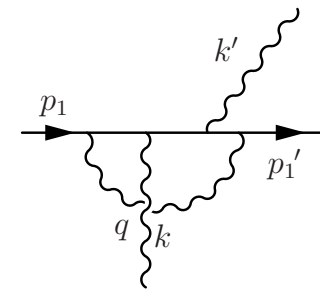
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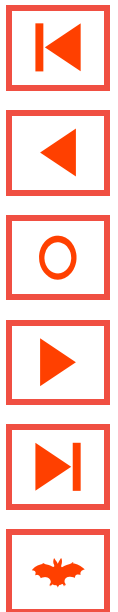
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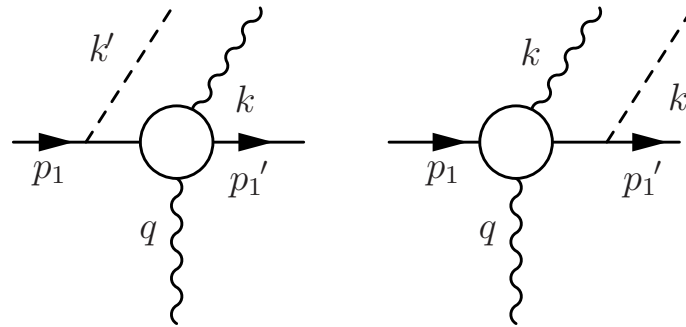


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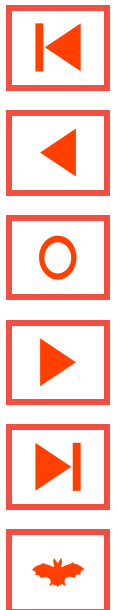
$$\begin{aligned}
 d\sigma^e &= 2[d\tau_{i,V}^{e,+ \pm} + d\tau_{i,\Sigma}^{e,+ \pm} + d\tau_{i,V}^{e,+ \pm} + d\tau_{i,box}^{e,+ \pm}] + d\tau_{e,soft}^{+ \pm} \\
 &= d\tau_B^{e,+ \pm} \frac{\alpha}{2\pi} [(l_u - 1)(4 \ln \Delta + 3 - 2 \ln \chi') + K_{SV}^{e,+ \pm}], \\
 l_{\chi'} &= \ln(\chi'/m^2) - i\pi^2
 \end{aligned}$$

– K factor – next-to-leading terms

Contribution of hard photon emission

$$\text{parameter } \theta_0 \ (\theta_0 \ll 1) \left\{ \begin{array}{l} \theta < \theta_0, \quad \text{collinear kinematics} \\ \theta > \theta_0, \quad \text{noncollinear kinematics} \end{array} \right. \begin{array}{l} \text{CALCUL collaboration,} \\ \text{quasi-real electron method} \end{array}$$

- total sum is independent on the parameter θ_0
- next-to-leading terms depend on experimental setup (included in K -factors)
- K -factors are free of infrared and collinear divergences (are independent of λ , Δ and θ_0)



Results

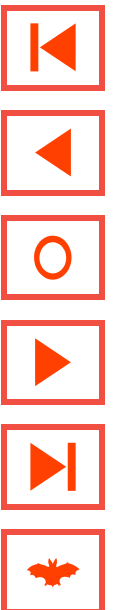
γ impact factor

$$d\tau^{\gamma, \lambda\sigma}(q_-, q_+) = \int_{x_-}^1 \frac{dz_-}{z_-} \int_{x_+}^1 \frac{dz_+}{z_+} D\left(\frac{x_-}{z_-}, l_s\right) D\left(\frac{x_+}{z_+}, l_s\right) d\tau_B^{\gamma, \lambda\sigma}\left(\frac{q_-}{z_-}, \frac{q_+}{z_+}\right) \\ \times \left(1 + \frac{\alpha}{\pi} [K_{SV}^{\gamma, \lambda\sigma} + K_{\text{coll}}^{-, \gamma} + K_{\text{coll}}^{+, \gamma} + K_{\text{ncol}}^{\gamma}]\right),$$

D – non-singlet structure function of fermion

$$D(z, l) = \delta(z - 1) + \frac{\alpha}{2\pi} (l - 1) P^{(1)}(z) + \dots$$

$$P^{(1)}(z) = \left(\delta(1 - z) \left(2 \ln \Delta + \frac{3}{2}\right) + \theta(1 - z - \Delta) \frac{1 + z^2}{1 - z} \right)_{\Delta \rightarrow 0}$$



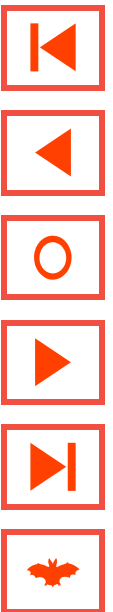
electron impact factor

$$\begin{aligned}
 d\tau^{e,\sigma\lambda}(p_1, p'_1) &= \int_0^1 dz_1 \int_{x'}^1 \frac{dz_2}{z_2} D(z_1, l_u) D\left(\frac{x'}{z_2}, l_u\right) d\tau_B^{e,\sigma\lambda}\left(z_1 p_1, \frac{p'_1}{z_2}\right) \\
 &\times \left(1 + \frac{\alpha}{\pi} [K_{SV}^{e,\sigma\lambda} + K_{\text{coll}}^{i,e} + K_{\text{coll}}^{f,e} + K_{\text{ncoll}}^e]\right),
 \end{aligned}$$

D – non-singlet structure function of fermion

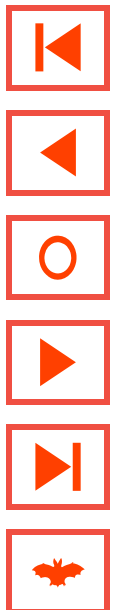
$$D(z, l) = \delta(z - 1) + \frac{\alpha}{2\pi} (l - 1) P^{(1)}(z) + \dots$$

$$P^{(1)}(z) = \left(\delta(1 - z) \left(2 \ln \Delta + \frac{3}{2}\right) + \theta(1 - z - \Delta) \frac{1 + z^2}{1 - z} \right)_{\Delta \rightarrow 0}$$



Conclusions

- We calculated **helicity amplitudes** for two-jet processes in **quasiperipheral kinematics** at Born and 1-loop correction levels.
- Contributions of the emission of virtual, soft and hard real additional photons were taken into account in construction of e, γ **impact factors** in the leading logarithmic approximation.
- The relevant **cross sections** were introduced in terms of structure functions for any helicity states of initial and final particles.
- We've presented K -factors (next-to-leading terms) in analytic form.
- Results were **validated** by gauge-invariance check.



Thank You for attention

